



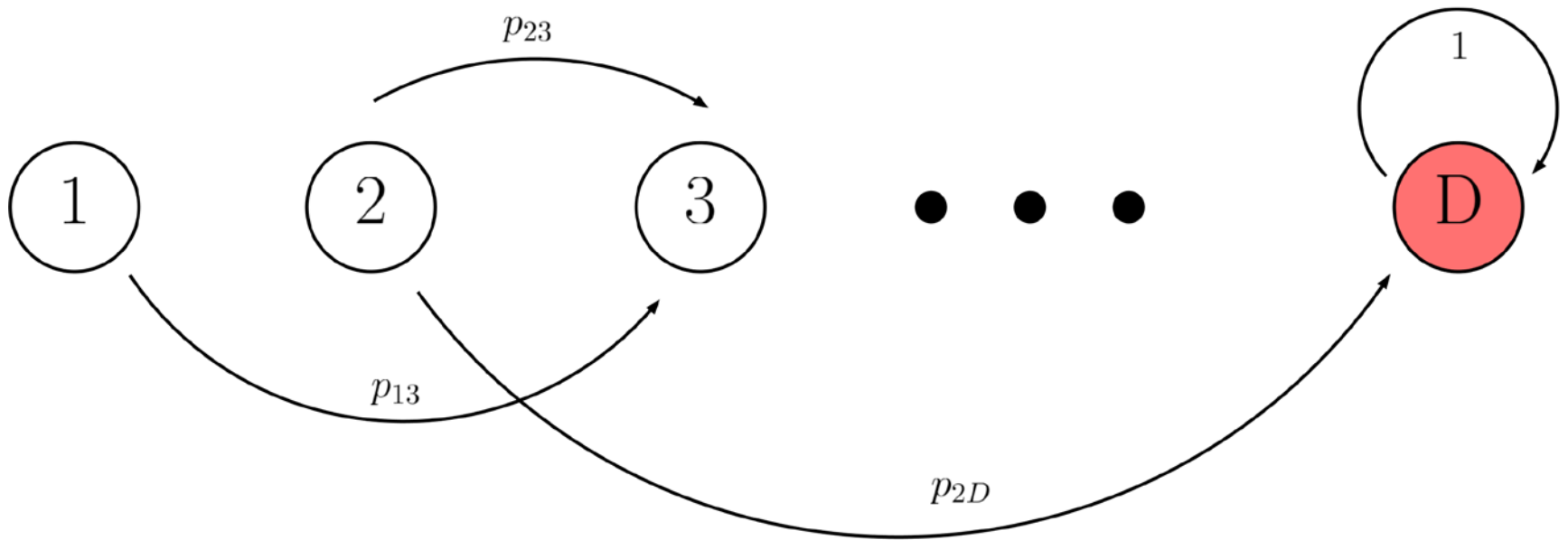
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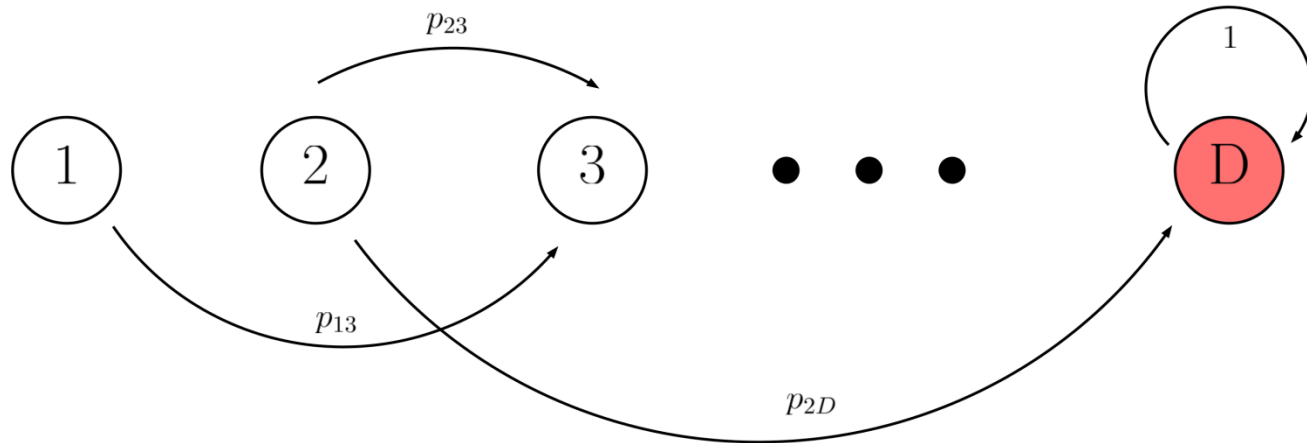
# Modeling Disk Failures with Absorbing Markov Chains

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# What is a Markov Chain?



# Terminology



**State Space:** the set of possible states the process can reach

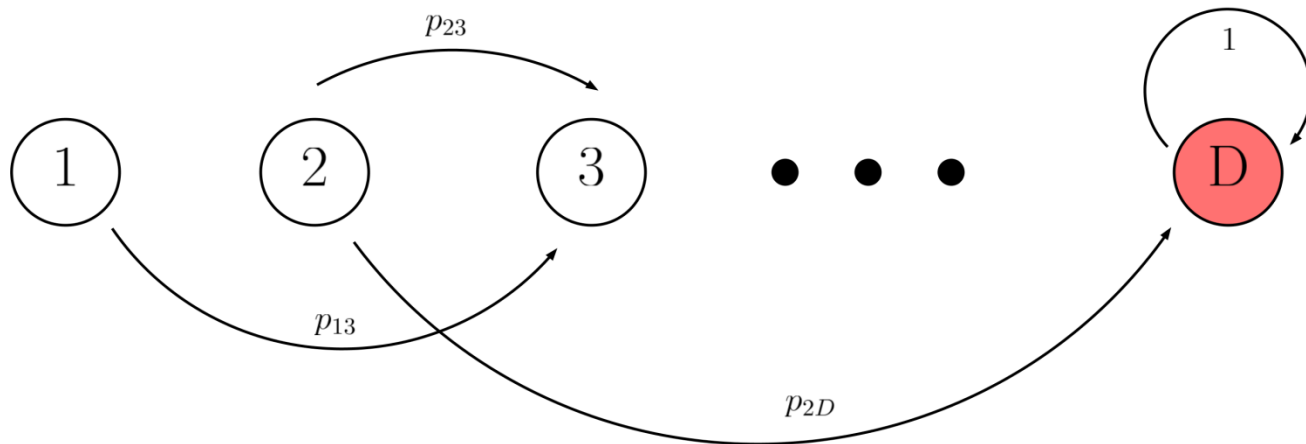
**Transition Probability ( $p_{ij}$ ):** the probability the process transitions from state  $i$  to state  $j$  in one step

**Absorbing State:** a state that, once entered, can never be left.

# Transition Matrix

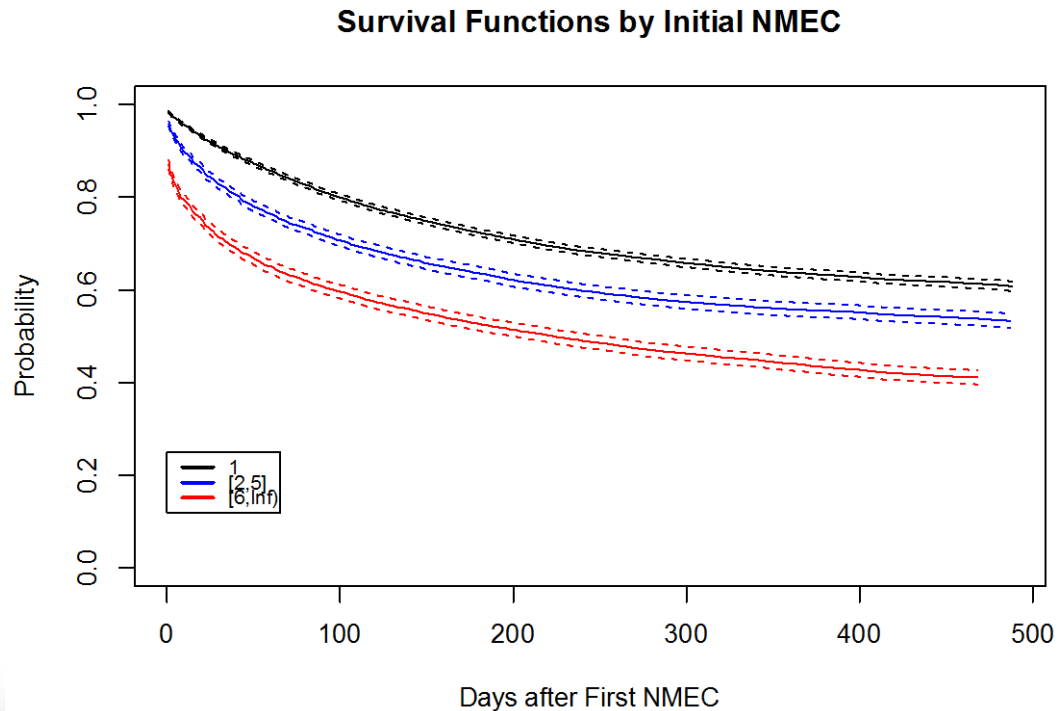
$$\begin{bmatrix} p_{11} & p_{12} & p_{13} & \cdots & p_{1D} \\ 0 & p_{22} & p_{23} & \cdots & p_{2D} \\ 0 & 0 & p_{33} & \cdots & p_{3D} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \cdots & 0 & 1 \end{bmatrix}$$

- For failure modeling, error counts always increase, so for  $j < i$ ,  $p_{ij} = 0$
- Note that the diagram below does not depict all possible transitions given in the matrix



# Modeling Medium Error Evolution

- **Medium error:** physical issue on the drive was encountered during access attempt
  - most commonly head error
- Medium Errors have been shown to be a good predictor of HDD failure.
- They are fairly rare in the field—approximately 1% of disks experience medium errors
- Conditioning on the initial NMEC, we see a decrease in survival rates fairly quickly



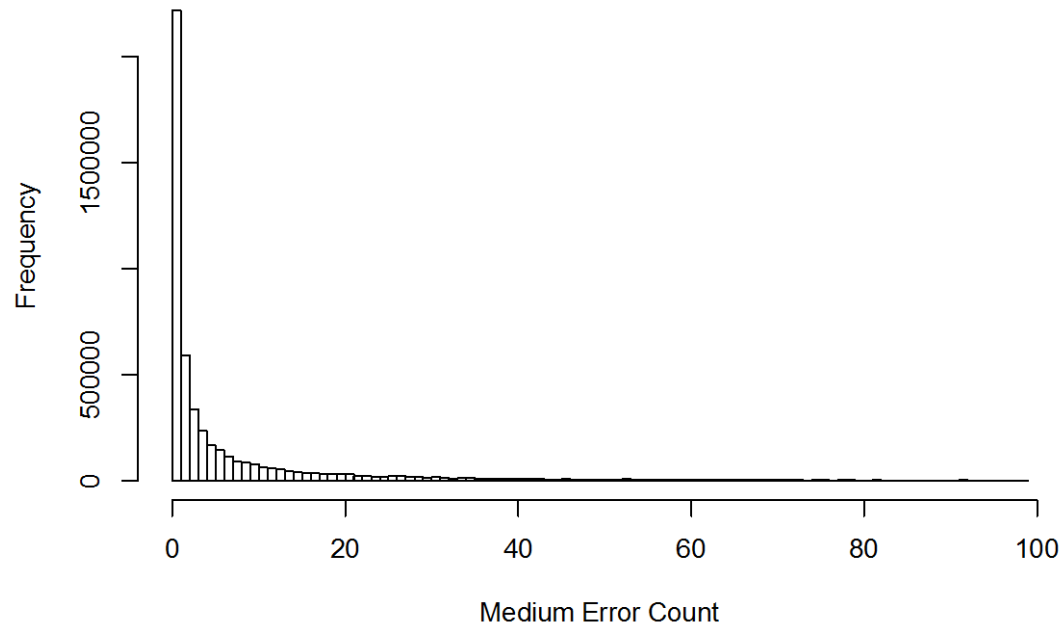
# Methodology-Conditional Markov Chain

- Create transition matrix conditioning on the existence of medium errors
- Let  $\tau$  be a transition. Then

$$P_{ij} = \frac{|\{\tau : ME = j\}|}{|\{\tau : ME_{prev} = i\}|}$$

# Binning

Distribution of Medium Errors < 100



- A Markov chain remains such even when condensing states
- Empirical bins were used to condense the state space to produce a more manageable transition matrix

Min	Q1	Med	Q3	Max
1	1	4	20	144250

# Beyond the Transition Probabilities

- ❑ The transition matrix simply gives the probability of moving from State  $i$  to State  $j$
- ❑ The transition matrix be used to answer many deeper questions about the evolution of the state space



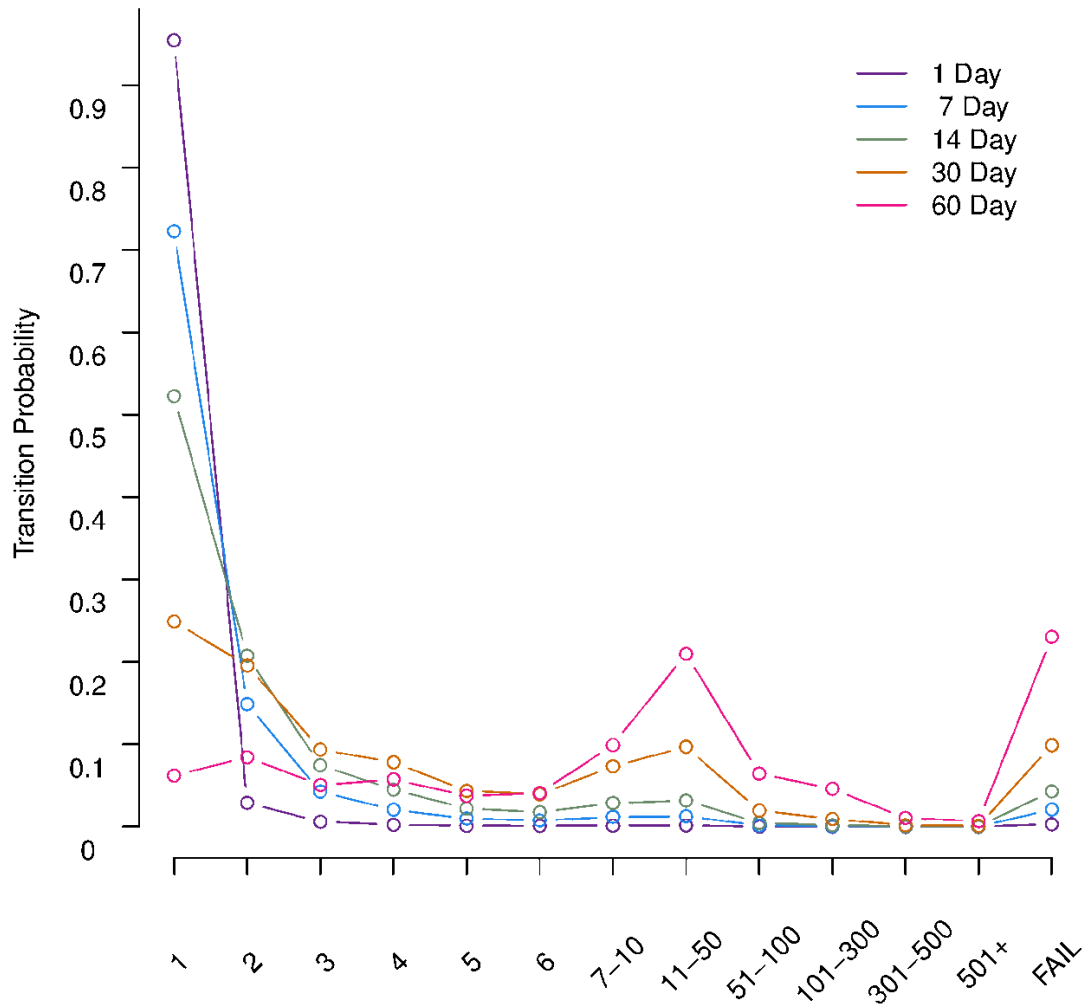
# N-step transition probabilities

- ❑ Of greater interest is the probability of transitioning from to State  $j$  in  $N$  steps, given that the process began in State  $i$
- ❑ The Markov process is memoryless
  - ❑ The information contained in the process's entire past is the same as the information contained in the previous step

$$P(X_n = x_n | X_{n-1} = x_{n-1}, \dots, X_0 = x_0) = P(X_n = x_n | X_{n-1} = x_{n-1})$$

- ❑ So, we may assume the day of observation is the “start” of a new process.

## Transition Probabilities Starting from 1 Medium Errors



The N-step transition probabilities are given by the entries of the matrix

$$P^N$$

## Other uses for the transition matrix

What is the probability that a disk with 3 medium errors today will have more than 10 medium errors in 7 days?

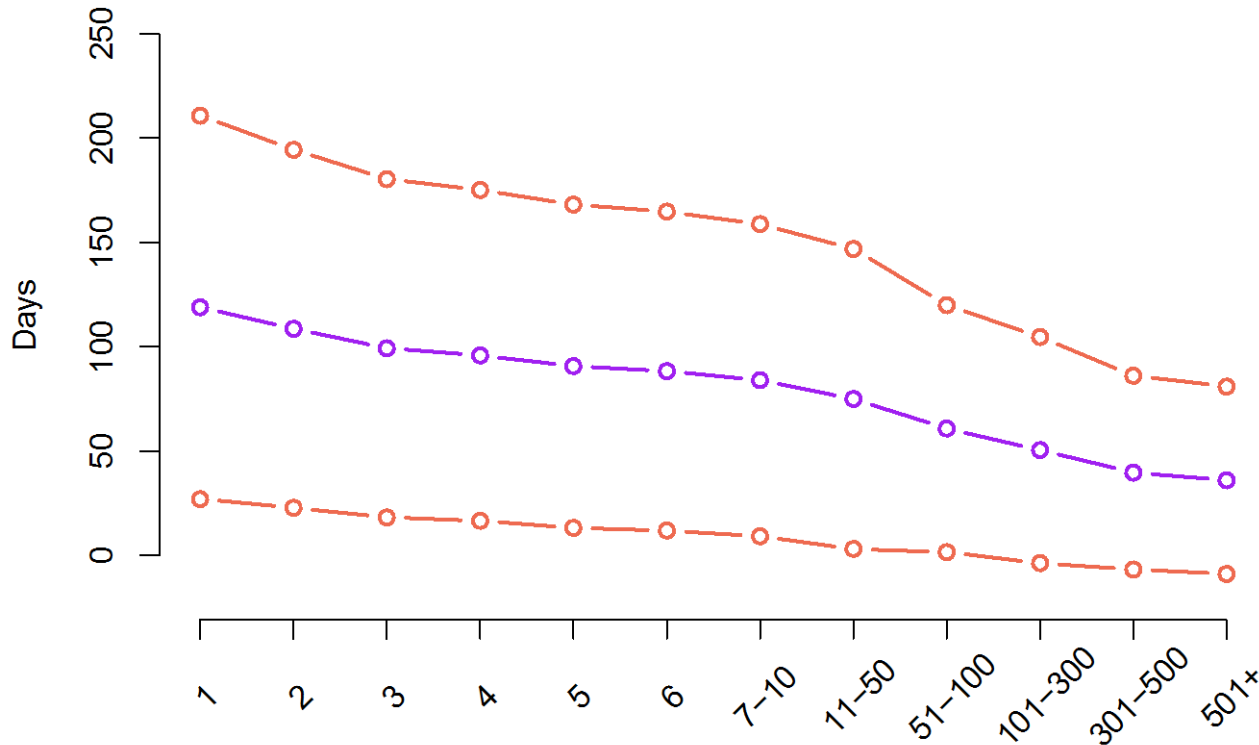
- The timestep is 7 days –  $\mathbf{P}^7$
- The current state is 3 medium errors

$$P(ME_{7>} > 10 | ME_c = 3) = p_{3,8}^{(7)} + p_{3,9}^{(7)} + p_{3,10}^{(7)} + p_{3,11}^{(7)} + p_{3,12}^{(7)} + p_{3,D}^{(7)} = 0.074$$

# Expected Time to Absorption

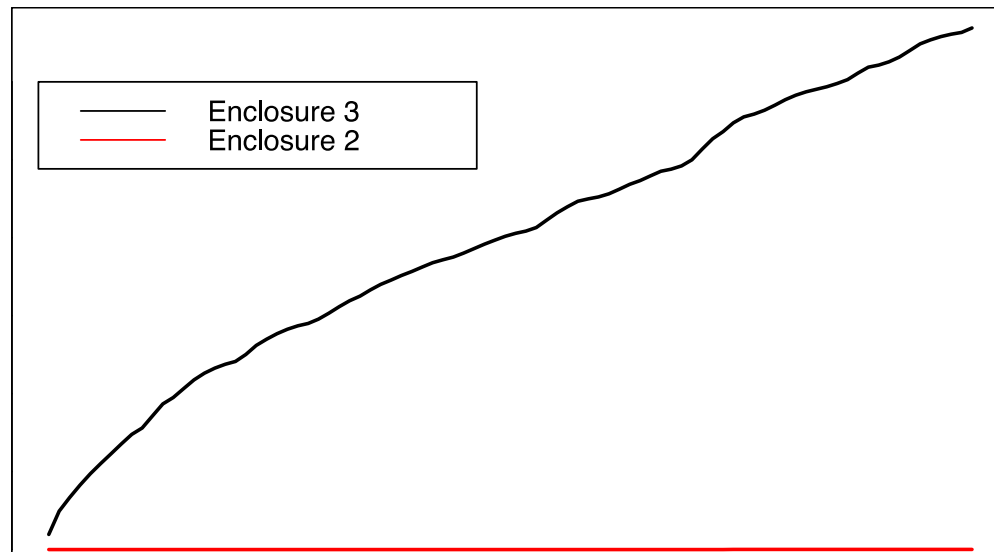
$$E[T] = (I - Q)^{-1} \mathbf{1}$$

Time to Absorption

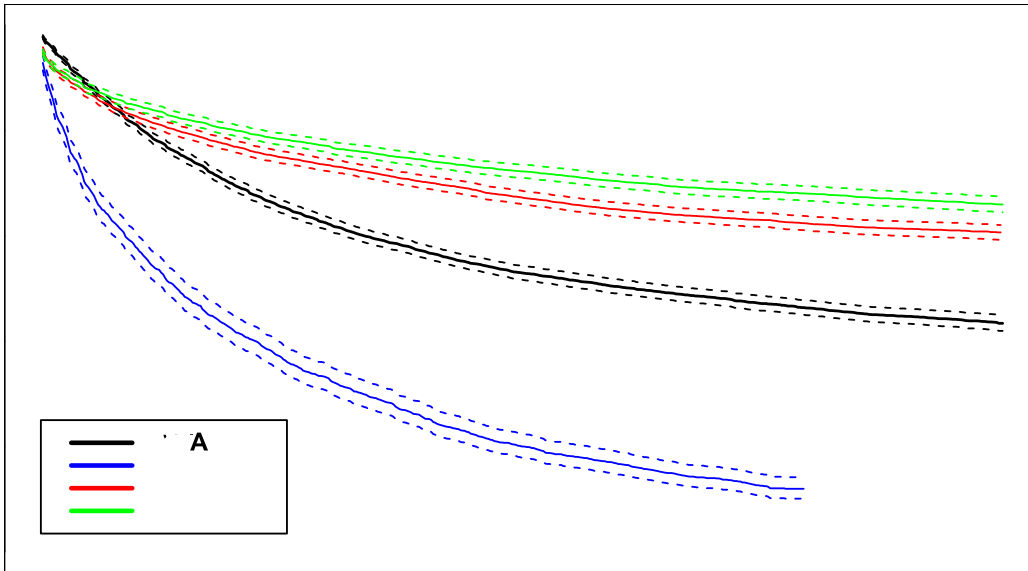


# Applications: RAID Group Risk algorithm

- The results of Markov chain modeling were used to develop an algorithm to predict the risk of data loss in a RAID group



# Other Applications



- State Space used for profiling
- Multidimensional/continuous Markov chain

# Conclusions

- ❑ Probabilistic foundation
- ❑ Computationally cheap, requires little updating
- ❑ Requires less data to maintain/evaluate
- ❑ Elegant and interpretable
- ❑ Compact form still allows for a wide variety of questions to be answered

# Questions?

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